

EN.553 (APPLIED MATHEMATICS & STATISTICS)

Courses

EN.553.100. Introduction to Applied Mathematics and Statistics. 1 Credit.

A seminar-style series of lectures and assignments to acquaint the student with a range of intellectual and professional activities performed by applied mathematicians and statisticians. Problems arising in applied mathematics and statistics are presented by department faculty and outside speakers. Recommended Course Background: one semester of Calculus.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.101. Freshman Experience in Applied Mathematics & Statistics. 1 Credit.

The aim of this course is to provide students with an opportunity to work on a project in a small group setting together with an AMS faculty member. Projects can be varied in nature depending on the faculty member working with a group. The goal of a group could be to develop knowledge of a domain area in which mathematics is applied, to develop knowledge of some technique(s) in applied mathematics, to bring applied mathematics to bear on some application, or to develop knowledge in some foundational topic in mathematics. Faculty will present possible topics to students in the first week of classes. Students will be asked to rank their interests (first choice, second choice, etc.), and will provide their schedules. Based on their preferences, their schedules, and subject to group size limitations, students will be organized into groups of size at most 3, and will be assigned to course sections in the second week of classes. One faculty member will lead each section and will arrange to meet with the group once per week for an hour.

Area: Quantitative and Mathematical Sciences

EN.553.111. Statistical Analysis I. 4 Credits.

First semester of a general survey of statistical methodology. Topics include descriptive statistics, introductory probability, conditional probability, random variables, expectation, sampling, the central limit theorem, classical and robust estimation, confidence intervals, and hypothesis testing. Case studies from psychology, epidemiology, economics and other fields serve to illustrate the underlying theory. Some use of Minitab, Excel or R, but no prior computing experience is necessary. Recommended Course Background: four years of high school mathematics. Students who may wish to undertake more than two semesters of probability and statistics should consider EN.553.420-EN.553.430.

Prerequisite(s): Statistics Sequence restriction: students who have completed AS.230.205 may not enroll.; Statistics Sequence restriction: students who have completed any of these courses may not register. EN.553.211 OR EN.553.230 OR EN.553.310 OR EN.553.311 OR EN.553.420 OR EN.553.421 OR EN.553.430 OR EN.553.413 OR EN.560.435 OR AS.280.345 OR AS.200.314 OR AS.200.315 OR EN.560.348

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.112. Statistical Analysis II. 4 Credits.

Second semester of a general survey of statistical methodology. Topics include two-sample hypothesis tests, analysis of variance, linear regression, correlation, analysis of categorical data, and nonparametrics. Students who may wish to undertake more than two semesters of probability and statistics should strongly consider the EN.553.420-430 sequence.

Prerequisite(s): EN.553.111 OR AS.230.205 OR AS.280.345 OR credit for AP Statistics

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.122. Chance and Risk. 3 Credits.

The course is intended for humanities and social science majors. It will help students develop an appreciation of probability and randomness, and an understanding of its applications in real life situations involving chance and risk. Applications, controversies, and paradoxes involving risk in business and economics, health and medicine, law, politics, sports, and gambling will be used to illustrate probabilistic concepts such as independence, conditional probability, expectation, correlation, and variance. Class periods will typically include a combination of presentation of new material, an in-class activity, and class discussion. Attendance and class participation will be an important part of the learning experience. Prerequisites: There is no prerequisite beyond high school mathematics. The course is not open to students who have taken calculus.

Prerequisite(s): Students may not have completed AS.110.106 OR AS.110.107 OR AS.110.108 OR AS.110.109 OR AS.110.113 OR AS.110.202 OR AS.110.211

Area: Quantitative and Mathematical Sciences

EN.553.171. Discrete Mathematics. 4 Credits.

Introduction to the mathematics of finite systems. Logic; Boolean algebra; induction and recursion; sets, functions, relations, equivalence, and partially ordered sets; elementary combinatorics; modular arithmetic and the Euclidean algorithm; group theory; permutations and symmetry groups; graph theory. Selected applications. The concept of a proof and development of the ability to recognize and construct proofs are part of the course. Recommended Course Background: Four years of high school mathematics.

Prerequisite(s): Students may only earn credit for one of the following: EN.553.171, EN.553.172, OR EN.601.230. EN.553.171 may not be taken after EN.553.471 OR EN.553.472 OR EN.553.671 OR EN.553.672.

Corequisite(s): EN.553.171 may not be taken concurrently with EN.553.471 or EN.553.472 or EN.553.671 or EN.553.672.

Area: Quantitative and Mathematical Sciences

EN.553.172. Honors Discrete Mathematics. 4 Credits.

Introduction to the mathematics of finite systems. Logic; Boolean algebra; induction and recursion; sets, functions, relations, equivalence, and partially ordered sets; elementary combinatorics; modular arithmetic and the Euclidean algorithm; polynomials rings, group theory; permutations groups and Galois theory; graph theory. Selected applications. The concept of a proof and development of the ability to recognize and construct proofs and analyze algorithms are part of the course. Recommended Course Background: Four years of high school mathematics.

Prerequisite(s): Students may only earn credit for one of the following: EN.553.171, EN.553.172, OR EN.601.230. EN.553.172 may not be taken after EN.553.471 OR EN.553.472 OR EN.553.671 OR EN.553.672.

Area: Quantitative and Mathematical Sciences

EN.553.211. Probability and Statistics for the Life Sciences. 4 Credits.

This is an introduction to statistics aimed at students in the life sciences. The course will provide the necessary background in probability with treatment of independence, Bayes theorem, discrete and continuous random variables and their distributions. The statistical topics covered will include sampling and sampling distributions, confidence intervals and hypothesis testing for means, comparison of populations, analysis of variance, linear regression and correlation. Analysis of data will be done using Excel.

Prerequisite(s): AS.110.106[C] OR AS.110.107[C] OR AS.110.108[C] OR AS.110.109[C] OR AS.110.113[C]; Statistics Sequence restriction: Students who have completed any of these courses may not register. EN.550.230 OR AS.280.345 OR AS.200.314 OR AS.200.315 OR EN.550.310 OR EN.550.311 OR EN.560.435 OR EN.550.420 OR EN.550.430 OR EN.560.348

Area: Quantitative and Mathematical Sciences

EN.553.230. Introduction to Biostatistics. 4 Credits.

A self-contained course covering various data analysis methods used in the life sciences. Topics include types of experimental data, numerical and graphical descriptive statistics, concepts of (and distinctions between) population and sample, basic probability, fitting curves to experimental data (regression analysis), comparing groups in populations (analysis of variance), methods of modeling probability (contingency tables and logistic regression). Prerequisite: 3 years of high school mathematics

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.281. Introduction to Mathematical Computing. 4 Credits.

This course introduces a variety of techniques for solving optimization problems in engineering and science on a computer using MATLAB. Topics include the programming language MATLAB, as well as optimization theory, algorithms, and applications. MATLAB optimization tools will also be explored. Algorithms to be covered will include gradient descent, Newton's method, and the simplex method. Applications will include constrained least squares regression, neural networks, and k-means clustering.

Prerequisite(s): (AS.110.107 OR AS.110.109 OR AS.110.113) AND (AS.110.201 OR AS.110.212 OR EN.553.291 OR EN.553.295)

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.291. Linear Algebra and Differential Equations. 4 Credits.

An introduction to the basic concepts of linear algebra, matrix theory, and differential equations that are used widely in modern engineering and science. Intended for engineering and science majors whose program does not permit taking both AS.110.201 and AS.110.302.

Prerequisite(s): AS.110.107 OR AS.110.109 OR AS.110.113

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.295. Linear Algebra for Data Science. 4 Credits.

A thorough introduction to linear algebra, with a focus on applications to data science and statistics. Topics include linear algebra in Euclidean spaces: matrices, vectors, linear independence, determinants, subspaces, bases, change of coordinates, linear transformations, null spaces and ranges, projections, orthogonalization, eigenvalues and eigenvectors; as well as least-squares approximation, spectral decomposition, quadratic forms, convexity, principal component analysis, dimensionality reduction, and approximation in function spaces. Matlab will be used for computation and applications. Prerequisites: AS.110.107 OR AS.110.109 OR AS.110.113

Prerequisite(s): AS.110.107 OR AS.110.109 OR AS.110.113

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.310. Probability & Statistics for the Physical Sciences & Engineering. 4 Credits.

An introduction to probability and statistics at the calculus level, intended for engineering and science students planning to take only one course on the topics. Combinatorial probability, independence, conditional probability, random variables, expectation and moments, limit theory, estimation, confidence intervals, hypothesis testing, tests of means and variances, goodness-of-fit. Recommended co-requisite: multivariable calculus. Students who have received credit for AS.110.106 and/or AS.110.107 taken prior to Fall 2020 should contact the course instructor to determine whether they can receive permission to register for this course.

Prerequisite(s): AS.110.109 OR AS.110.113; Statistics Sequence restriction: Students who have completed any of these courses may not register. EN.553.311 OR EN.560.435 OR EN.553.420 OR EN.553.421 OR EN.553.430 OR EN.560.348

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.311. Intermediate Probability and Statistics. 4 Credits.

An introduction to probability and statistics at the calculus level, intended for students in the biological sciences planning to take only one course on the topics. This course will be at the same technical level as EN.553.310. Students are encouraged to consider EN.553.420-430 instead. Combinatorial probability, independence, conditional probability, random variables, expectation and moments, limit theory, estimation, confidence intervals, hypothesis testing, tests of means and variances, and goodness-of-fit will be covered. Students who have received credit for AS.110.106 and/or AS.110.107 taken prior to Fall 2020 should contact the course instructor to determine whether they can receive permission to register for this course. Recommended Course Corequisite: AS.110.202

Prerequisite(s): AS.110.109 OR AS.110.113; Statistics Sequence restriction: students who have completed any of these courses may not register. EN.553.310 OR EN.560.435 OR EN.553.420 OR EN.553.421 OR EN.553.430 OR EN.560.348

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.335. Mathematics for a Better World. 3 Credits.

The content of this course is jointly developed and delivered by the instructor and a community partner under the auspices of the JHU Center for Social Concern. Bmore Community Food founder J.C. Faulk and the instructor will co-teach a course designed to provide students with: (1) insights to creating and operating of a community food shelf, (2) experience in utilizing mathematical knowledge to support the operation of the food shelf. Topics of discussion includes community organization, governance, transparency, grants, and donor. Technical aspects of the course will include building a dashboard for the organization that will allow for improved access to information, and provide analytics. The class will meet weekly with site visits to Bmore Community Food, and may include service. Prerequisites: Python, basic statistics and visualization; knowledge of databases desirable.

EN.553.361. Introduction to Optimization. 4 Credits.

An introductory survey of optimization methods, supporting mathematical theory and concepts, and application to problems of planning, design, prediction, estimation, and control in engineering, management, and science. Study of varied optimization techniques including linear programming, network-problem methods, dynamic programming, integer programming, and nonlinear programming. Students should be familiar with computing and linear algebra. Prerequisite: one year of calculus. Students who have received credit for AS.110.106 and/or AS.110.107 taken prior to Fall 2020 should contact the course instructor to determine whether they can receive permission to register for this course.

Prerequisite(s): (AS.110.109 OR AS.110.113) AND (EN.553.291 OR EN.553.295 OR AS.110.201 OR AS.110.212)

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.362. Introduction to Optimization II. 4 Credits.

An introductory survey of optimization methods, supporting mathematical theory and concepts, and application to problems of planning, design, prediction, estimation, and control in engineering, management, and science. Study of varied optimization techniques including linear programming, network-problem methods, dynamic programming, integer programming, and nonlinear programming.

Prerequisite(s): EN.550.361 AND (AS.110.202 OR AS.110.211)

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.371. Cryptology and Coding. 4 Credits.

Computing experience. A first course in the mathematical theory of secure and reliable electronic communication. Cryptology is the study of secure communication: How can we ensure the privacy of messages? Coding theory studies how to make communication reliable: How can messages be sent over noisy lines? Topics include finite field arithmetic, error-detecting and error-correcting codes, data compressions, ciphers, one-time pads, the Enigma machine, one-way functions, discrete logarithm, primality testing, secret key exchange, public key cryptosystems, digital signatures, and key escrow.

Prerequisite(s): EN.553.172 AND (EN.553.291 OR EN.553.295 OR AS.110.201 OR AS.110.212)

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.385. Introduction to Computational Mathematics. 4 Credits.

This course offers a broad introduction to the area of numerical computation in the mathematical sciences. Topics include but may not be limited to: floating point numbers, linear systems, LU factorization, vector and matrix norms, conditioning of linear systems, QR factorizations, the root finding problem, fixed point iterations, Newton's method in one variable and for nonlinear systems, interpolation, cubic splines, finite differences, numerical integration, initial-value problems for ODEs, Euler's method, systems of differential equations, Runge-Kutta methods, eigenvalue and singular value decomposition of matrices, polynomial approximation, shooting methods for boundary-value problems; time permitting: basic finite-difference methods for the solution of PDEs. The prerequisites are linear algebra, multivariable calculus, and differential equations; however, the latter may be taken concurrently.

Prerequisite(s): (EN.553.291 OR EN.553.295 OR AS.110.201 OR AS.110.212) AND (AS.110.202 OR AS.110.211)

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.386. Scientific Computing: Differential Equations. 4 Credits.

A first course on computational differential equations and applications. Topics include floating-point arithmetic, algorithms and convergence, root-finding (midpoint, Newton, and secant methods), numerical differentiation and integration, and numerical solution of initial value problems (Runge–Kutta, multistep, extrapolation methods, stability, implicit methods, and stiffness). Theoretical topics such as existence, uniqueness, and stability of solutions to initial-value problems, conversion of higher order/ non-autonomous equations to systems, etc., will be covered as needed. Matlab is used to solve all numerical exercises; no previous experience with computer programming is required.

Prerequisite(s): (AS.110.202 OR AS.110.211) AND (EN.553.291 OR AS.110.302 OR AS.110.306).

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.391. Dynamical Systems. 4 Credits.

Mathematical concepts and methods for describing and analyzing linear and nonlinear systems that evolve over time. Topics include boundedness, stability of fixed points and attractors, feedback, optimality, Liapounov functions, bifurcation, chaos, and catastrophes. Examples drawn from population growth, economic behavior, physical and engineering systems. The main mathematical tools are linear algebra and basic differential equations.

Prerequisite(s): EN.553.291 OR EN.553.295 OR AS.110.201 OR AS.110.211

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.400. Mathematical Modeling and Consulting. 4 Credits.

Creating, analyzing and evaluating optimization and mathematical models using case studies. Project-oriented practice and guidance in modeling techniques, with emphasis on communication of methods and results. Applications may include transportation networks, scheduling, industrial processes, and telecommunications. Computation will be emphasized throughout using MATLAB.

Prerequisite(s): EN.553.361 OR EN.553.362; Students may receive credit for EN.550.400/EN.553.400 or EN.553.600, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.401. Introduction to Research. 3 Credits.

This course will provide students with a comprehensive hands-on introduction to the research process, which includes performing a literature survey, mathematical modeling, theoretical, numerical, and/or empirical approaches while solving some of the problems in the research landscape. Some topics include (but are unlimited to) the following: • Systems Reliability Analysis • Systems Management • Network Analysis • Sports Scheduling • 5-G (and Next-Gen) Explorations • Mechanical Ventilation Data Analysis and Management In the process, students will have the experience to produce their status reports and results orally and in writing where the goal is to provide an initial working publication that can be extended for upcoming conference and/or journal submissions.

Area: Quantitative and Mathematical Sciences

EN.553.402. Research and Design in Applied Mathematics: Data Mining. 4 Credits.

The course will be project oriented with focus on practical uses of machine learning and data mining. Throughout the semester, teams of 4 will work on topics decided by the students and the instructor.

Prerequisite(s): EN.553.436

Area: Quantitative and Mathematical Sciences

EN.553.413. Applied Statistics and Data Analysis. 4 Credits.

An introduction to basic concepts, techniques, and major computer software packages in applied statistics and data analysis. Topics include numerical descriptive statistics, observations and variables, sampling distributions, statistical inference, linear regression, multiple regression, design of experiments, nonparametric methods, and sample surveys. Real-life data sets are used in lectures and computer assignments. Intensive use of statistical packages such as R to analyze data.

Prerequisite(s): Students may receive credit for EN.550.413/EN.553.413 or EN.553.613, but not both.;EN.553.112 OR EN.553.310 OR EN.553.311 OR EN.553.420 OR EN.553.421

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.414. Applied Statistics and Data Analysis II. 3 Credits.

Part II of a sequence on data analysis and linear models. Topics include categorical and discrete data analysis, mixed models, semiparametric and nonparametric regression, and generalized additive models. Applications of these methods using the R environment for statistical computing will be emphasized.

Prerequisite(s): EN.550.413;Students may receive credit for EN.550.414/ EN.553.414 or EN.553.614, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.420. Probability. 4 Credits.

Probability and its applications, at the calculus level. Emphasis on techniques of application and on rigorous mathematical demonstration. Probability, combinatorial probability, random variables, distribution functions, important probability distributions, independence, conditional probability, moments, covariance and correlation, limit theorems. Students initiating graduate work in probability or statistics should enroll in EN.553.620 or EN.553.720. Prerequisites: one year of calculus. Corequisites: multivariable calculus and linear algebra.Students who have received credit for AS.110.106 and/or AS.110.107 taken prior to Fall 2020 should contact the course instructor to determine whether they can receive permission to register for this course.

Prerequisite(s): Students may receive credit for one of the following: EN.550.420/EN.553.420 OR EN.553.421 OR EN.553.620.;AS.110.109 OR AS.110.113;AS.110.201 OR AS.110.202 OR AS.110.211 OR AS.110.212 OR EN.553.295, can be taken concurrently.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.421. Honors Introduction to Probability. 4 Credits.

Probability and its applications, at the calculus level. Emphasis on techniques of application and on rigorous mathematical demonstration. Probability, combinatorial probability, random variables, distribution functions, important probability distributions, independence, conditional probability, moments, exchangeability, joint distributions, conditional distributions and expectation, covariance and correlation, limit theorems. The honors version of this course will have enrichment exercises that explore and extend ideas learned in the ordinary lecture. Students initiating graduate work in probability or statistics should enroll in EN.550.620. Auditors are not permitted. Recommended Course Background: one year of calculus and mathematical maturity; Co-requisite: multivariable calculus. By permission of the instructor or by recommendation of an AMS faculty member.

Area: Quantitative and Mathematical Sciences

EN.553.426. Introduction to Stochastic Processes. 4 Credits.

Mathematical theory of stochastic processes. Emphasis on deriving the dependence relations, statistical properties, and sample path behavior including random walks, Markov chains (both discrete and continuous time), Poisson processes, martingales, and Brownian motion. Applications that illuminate the theory. Students may receive credit for EN.553.426 or EN.553.626.

Prerequisite(s): Students may receive credit for EN.550.426/EN.553.426 or EN.553.626, but not both.;(EN.553.420 OR EN.553.421 OR EN.553.620) AND (EN.553.291 OR EN.553.295 OR AS.110.201 OR AS.110.212)

Corequisite(s): Students may not enroll in EN.553.420 in the same semester.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.427. Stochastic Processes and Applications to Finance. 4 Credits.

A development of stochastic processes with substantial emphasis on the processes, concepts, and methods useful in mathematical finance. Relevant concepts from probability theory, particularly conditional probability and conditional expectation, will be briefly reviewed. Important concepts in stochastic processes will be introduced in the simpler setting of discrete-time processes, including random walks, Markov chains, and discrete-time martingales, then used to motivate more advanced material. Most of the course will concentrate on continuous-time stochastic processes, particularly martingales, Brownian motion, diffusions, and basic tools of stochastic calculus. Examples will focus on applications in finance, economics, business, and actuarial science.Students may only earn credit for one of EN.553.427 or EN.553.627.

Prerequisite(s): Students may receive credit for only one of EN.550.427, EN.553.427, OR EN.553.627;EN.553.420 OR EN.553.421 OR EN.553.620

Area: Quantitative and Mathematical Sciences

EN.553.428. Stochastic Processes and Applications to Finance II. 4 Credits.

A basic knowledge of stochastic calculus and Brownian motion is assumed. Topics include stochastic differential equations, the Feynman-Kac formula and connections to partial differential equations, changes of measure, fundamental theorems of asset pricing, martingale representations, first passage times and pricing of path-dependent options, and jump processes.

Prerequisite(s): EN.553.427 OR EN.553.627;Students may receive credit for EN.550.428/EN.553.428 or EN.553.628, but not both.

Area: Quantitative and Mathematical Sciences

EN.553.430. Mathematical Statistics. 4 Credits.

Introduction to mathematical statistics. Finite population sampling, approximation methods,classical parametric estimation, hypothesis testing, analysis of variance, and regression. Bayesian methods.

Prerequisite(s): Students may receive credit for EN.550.430/EN.553.430 or EN.553.630 or EN.553.431, but not all.;(EN.553.420 OR EN.553.421 OR EN.553.620) AND (AS.110.201 OR AS.110.212 OR EN.553.291 OR EN.553.295)

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.431. Honors Mathematical Statistics. 4 Credits.

Introduction to the theory and methodology of mathematical statistics: parametric estimation, including asymptotic properties of estimators and approximation methods; hypothesis testing; analysis of variance; regression; bootstrapping and nonparametrics. Intended for students with a particular interest in the theoretical foundations of statistical procedures.

Prerequisite(s): Students may receive credit for only one of EN.553.430, EN.553.431 or EN.553.630.;(EN.553.420 OR EN.553.421 OR EN.553.620) AND (AS.110.201 OR AS.110.212 OR EN.553.291 OR EN.553.295) AND (AS.110.202 OR AS.110.211)

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.432. Bayesian Statistics. 3 Credits.

The course will cover Bayesian methods for exploratory data analysis. The emphasis will be on applied data analysis in various disciplines. We will consider a variety of topics, including introduction to Bayesian inference, prior and posterior distribution, hierarchical models, spatial models, longitudinal models, models for categorical data and missing data, model checking and selection, computational methods by Markov Chain Monte Carlo using R or Matlab. We will also cover some nonparametric Bayesian models if time allows, such as Gaussian processes and Dirichlet processes.

Prerequisite(s): Students may take only one of EN.550.632, EN.553.432, EN.553.632 or EN.553.732.;(EN.553.420 OR EN.553.421 OR EN.553.620) AND (EN.553.430 OR EN.553.431 OR EN.553.630)

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.433. Monte Carlo Methods. 4 Credits.

The objective of the course is to survey essential simulation techniques for popular stochastic models. The stochastic models may include classical time-series models, Markov chains and diffusion models. The basic simulation techniques covered will be useful in sample-generation of random variables, vectors and stochastic processes, and as advanced techniques, importance sampling, particle filtering and Bayesian computation may be discussed.

Prerequisite(s): Students may receive credit for EN.553.433 or EN.553.633, but not both.;EN.553.430 OR EN.553.431 OR EN.553.630
Area: Engineering, Quantitative and Mathematical Sciences

EN.553.436. Introduction to Data Science. 4 Credits.

Today the term Data Science is widely used covering a broad range of topics from mathematics and algorithms to actual data analysis and machine learning techniques. This course provides a thorough survey of relevant methods balancing the theory and the application aspects. Accordingly, the material and the discussions alternate between the methodology along with its underlying assumptions and the implementations along with their applications. We will cover several supervised methods for regression and classification, as well as unsupervised methods for clustering and dimensional reduction. To name a few in chronological order, the topics will include generalized linear regression, principal component analysis, nearest neighbor and Bayesian classifiers, support vector machines, logistic regression, decision trees, random forests, K-means clustering, Gaussian mixtures and Laplacian eigenmaps. The course uses Python and Jupyter Notebook and includes visualization techniques throughout the semester. Time permitting, an introduction to the Structured Query Language (SQL) is provided toward the end of the semester.

Prerequisite(s): Students may receive credit for EN.550.436/EN.553.436 or EN.553.636, but not both.;(AS.110.202 OR AS.110.211) AND (AS.110.201 OR AS.110.212 OR EN.553.291 OR EN.553.295)

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.439. Time Series Analysis. 3 Credits.

Time series analysis from the frequency and time domain approaches. Descriptive techniques; regression analysis; trends, smoothing, prediction; linear systems; serial correlation; stationary processes; spectral analysis.

Prerequisite(s): Students may receive credit for EN.553.439 or EN.553.639, but not both.;(EN.553.310 OR EN.553.311 OR EN.553.420 OR EN.553.421 OR EN.553.620) AND (AS.110.201 OR AS.110.212 OR EN.553.291 OR EN.553.295)

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.441. Equity Markets and Quantitative Trading. 3 Credits.

This course introduces equity markets from a mathematical point of view. The properties of equities and equity-linked instruments will be described. Several quantitative trading strategies will be studied. Order execution tactics and the effect of market structure will be analyzed. Students will select a specialized aspect of the equity markets to investigate and complete a related independent project.

Prerequisite(s): Students may receive credit for EN.550.441/EN.553.441 or EN.553.641, but not both.;EN.553.442 OR EN.553.642 or instructor's permission.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.442. Investment Science. 4 Credits.

This course offers a rigorous treatment of the subject of investment as a scientific discipline. Mathematics is employed as the main tool to convey the principles of investment science and their use to make investment calculations for good decision-making. Topics covered in the course include the basic theory of interest and its application to fixed-income securities, cash flow analysis and capital budgeting, mean-variance portfolio theory, and the associated capital asset pricing model, utility function theory and risk analysis, derivative securities and basic option theory, portfolio evaluation. The student is expected to be comfortable with the use of mathematics as a method of deduction and problem solving. Students may not receive credit for both EN.550.342 and EN.553.442. Students who have received credit for AS.110.106 and/or AS.110.107 taken prior to Fall 2020 should contact the course instructor to determine whether they can receive permission to register for this course.

Prerequisite(s): Students may receive credit for only one of EN.550.342, EN.550.442, EN.553.442 or EN.553.642.;(AS.110.109 OR AS.110.113) AND (EN.553.291 OR EN.553.295 OR AS.110.201 OR AS.110.212) AND (EN.553.310 OR EN.553.311 OR EN.553.420 OR EN.553.421 OR EN.553.620 OR EN.553.430 OR EN.553.431 OR EN.553.630)

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.444. Introduction to Financial Derivatives. 4 Credits.

This course will develop the mathematical concepts and techniques for modeling cash instruments and their hybrids and derivatives.

Prerequisite(s): Students may receive credit for EN.550.444/EN.553.444 or EN.553.644, but not both.;AS.110.302 AND (EN.553.420 OR EN.553.421)

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.445. Interest Rate and Credit Derivatives. 4 Credits.

Advances in corporate finance, investment practice and the capital markets have been driven by the development of a mathematically rigorous theory for financial instruments and the markets in which they trade. This course builds on the concepts, techniques, instruments and markets introduced in EN.553.444. In addition to new topics in credit enhancement and structured securities, the focus is expanded to include applications in portfolio theory and risk management, and covers some numerical and computational approaches.

Prerequisite(s): EN.553.444 OR EN.553.644; Students may receive credit for EN.550.445/EN.553.445 or EN.553.645, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.446. Risk Measurement/Management in Financial Markets. 4 Credits.

This course applies advanced mathematical techniques to the measurement, analysis, and management of risk. The focus is on financial risk. Sources of risk for financial instruments (e.g., market risk, interest rate risk, credit risk) are analyzed; models for these risk factors are studied and the limitation, shortcomings and compensatory techniques are addressed.

Prerequisite(s): Students may receive credit for EN.550.446/EN.553.446 or EN.553.646, but not both.; EN.553.444 OR EN.553.644

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.447. Quantitative Portfolio Theory and Performance Analysis. 4 Credits.

This course focuses on modern quantitative portfolio theory, models, and analysis. Topics include intertemporal approaches to modeling and optimizing asset selection and asset allocation; benchmarks (indexes), performance assessment (including, Sharpe, Treynor and Jensen ratios) and performance attribution; immunization theorems; alpha-beta separation in management, performance measurement and attribution; Replicating Benchmark Index (RBI) strategies using cash securities / derivatives; Liability-Driven Investment (LDI); and the taxonomy and techniques of strategies for traditional management: Passive, Quasi-Passive (Indexing) Semi-Active (Immunization & Dedicated) Active (Scenario, Relative Value, Total Return and Optimization). In addition, risk management and hedging techniques are also addressed.

Prerequisite(s): Students may receive credit for EN.550.447/EN.553.447 OR EN.553.647, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.448. Financial Engineering and Structured Products. 4 Credits.

This course focuses on structured securities and the structuring of aggregates of financial instruments into engineered solutions of problems in capital finance. Topics include the fundamentals of creating asset-backed and structured securities—including mortgage-backed securities (MBS), stripped securities, collateralized mortgage obligations (CMOs), and other asset-backed collateralized debt obligations (CDOs)—structuring and allocating cash-flows as well as enhancing credit; equity hybrids and convertible instruments; asset swaps, credit derivatives and total return swaps; assessment of structure-risk interest rate-risk and credit-risk as well as strategies for hedging these exposures; managing portfolios of structured securities; and relative value analysis (including OAS and scenario analysis).

Prerequisite(s): EN.553.442 OR EN.553.642 OR EN.553.444 OR EN.553.644; Students may receive credit for EN.550.448/EN.553.448 or EN.553.648, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.449. Advanced Equity Derivatives. 4 Credits.

This course will cover the pricing, trading and risk management of equity derivatives, with emphasis on more exotic derivatives such as path-dependent and multi-asset derivatives. The course will emphasize practical issues: students will build their own pricing and risk management tools, and gain experience simulating the dynamic hedging of a complex derivatives portfolio. Students will practice structuring and selling equity derivative products. Pricing issues such as model selection, unobservable input parameters and calibration will be discussed, and students will learn techniques to manage the often highly nonlinear and discontinuous risks associated with these products. The course will have a significant computing component: both in the classroom and as homework projects, students will use Excel, write VBA macros and write and call C++ routines in the Microsoft Windows environment (which is the most common computing environment used by the financial industry).

Prerequisite(s): Students may receive credit for EN.550.449/EN.553.449 or EN.553.649, but not both.; EN.553.444 OR EN.553.644

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.450. Computational Molecular Medicine. 4 Credits.

Computational systems biology has emerged as the dominant framework for analyzing high-dimensional “omics” data in order to uncover the relationships among molecules, networks and disease. In particular, many of the core methodologies are based on statistical modeling, including machine learning, stochastic processes and statistical inference. We will cover the key aspects of this methodology, including measuring associations, testing multiple hypotheses, and learning predictors, Markov chains and graphical models. In addition, by studying recent important articles in cancer systems biology, we will illustrate how this approach enhances our ability to annotate genomes, discover molecular disease networks, detect disease, predict clinical outcomes, and characterize disease progression. Whereas a good foundation in probability and statistics is necessary, no prior exposure to molecular biology is required (although helpful).

Prerequisite(s): Students may receive credit for EN.553.450 or EN.553.650, but not both.; (EN.553.420 OR EN.553.421 OR EN.553.620) AND (EN.553.430 OR EN.553.431 OR EN.553.630) OR equivalent courses in probability and statistics.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.453. Mathematical Game Theory. 4 Credits.

Mathematical analysis of cooperative and noncooperative games. Theory and solution methods for matrix game (two players, zero-sum payoffs, finite strategy sets), games with a continuum of strategies, N-player games, games in rule-defined form. The roles of information and memory. Selected applications to economic, recreational, and military situations. Prereq: Multivariable Calculus, probability, linear algebra.

Prerequisite(s): Students may receive credit for EN.550.453/EN.553.453 or EN.553.653, but not both.; (AS.110.202 OR AS.110.211) AND (EN.553.420 OR EN.553.620) AND (EN.553.291 OR EN.553.295 OR AS.110.201 OR AS.110.212)

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.461. Optimization in Finance. 4 Credits.

A survey of many of the more important optimization methods and tools that are found to be useful in financial applications.

Prerequisite(s): Students may receive credit for EN.550.461/EN.553.461 or EN.553.661, but not both.; EN.553.442 OR EN.553.642 OR EN.553.444 OR EN.553.644

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.463. Network Models in Operations Research. 4 Credits.

In-depth mathematical study of network flow models in operations research, with emphasis on combinatorial approaches for solving them. Introduction to techniques for constructing efficient algorithms, and to some related data structures, used in solving shortest-path, maximum-volume, flow, and minimum-cost flow problems. Emphasis on linear models and flows, with brief discussion of non-linear models and network design.

Prerequisite(s): Students may receive credit for EN.550.463/EN.553.463 or EN.553.663, but not both.;EN.553.361 OR EN.553.661 OR EN.553.761 OR EN.553.461

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.465. Introduction to Convexity. 4 Credits.

Convexity is a simple mathematical concept that has become central in a diverse range of applications in engineering, science and business applications. Our main focus from the applications perspective will be the use of convexity within optimization problems, where convexity plays a key role in identifying the "easy" problems from the "hard" ones. The course will have an equal emphasis on expositing the rich mathematical structure of the field itself (properties of convex sets, convex functions, Helly-Carathéodory-Radon type theorems, polarity/duality, subdifferential calculus, polyhedral theory), and demonstrating how these ideas can be leveraged to model and solve optimization problems (via a detailed study of linear programming and basics of nonlinear convex optimization). Recommend Course Background: Familiarity with basic real analysis, linear algebra.

Prerequisite(s): Students may receive credit for EN.550.465/EN.553.465 or EN.553.665, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.467. Deep Learning in Discrete Optimization. 3 Credits.

The goal of the course is to examine research-level topics in the application of deep-learning techniques to the solution of computational problems in discrete optimization. The first part of the course will cover background material, introducing students to deep learning (focusing on practical aspects) and covering major topics in computational discrete optimization: heuristic methods, dynamic programming, linear programming, cutting planes, column generation, and branch-and-bound. We will then make an in-depth study of research papers where deep learning has been proposed as a solution-technique in discrete optimization, aiming towards discussions of open research questions. Prerequisites: General mathematical maturity is expected: students should feel comfortable reading on their own Part 1 (Applied Math and Machine Learning Basics) in the text Deep Learning by Goodfellow, Bengio, and Courville.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.471. Combinatorial Analysis. 4 Credits.

Counting techniques: generating functions, recurrence relations, Polya's theorem. Combinatorial designs: Latin squares, finite geometries, balanced incomplete block designs. Emphasis on problem solving. Recommended Course Background: AS.553.291 or AS.110.201 Students who have received credit for AS.110.106 and/or AS.110.107 taken prior to Fall 2020 should contact the course instructor to determine whether they can receive permission to register for this course.

Prerequisite(s): Students may receive credit for EN.550.471/EN.553.471 or EN.550.671/EN.553.671, but not both.:(AS.110.109 OR AS.110.113) AND (AS.110.201 OR AS.110.212 OR EN.553.291 OR EN.553.295)

Corequisite(s): EN.553.171 may not be taken concurrently with EN.553.471, EN.553.472, EN.553.671, or EN.553.672.

Area: Quantitative and Mathematical Sciences

EN.553.472. Graph Theory. 4 Credits.

Study of systems of "vertices" with some pairs joined by "edges." Theory of adjacency, connectivity, traversability, feedback, and other concepts underlying properties important in engineering and the sciences. Topics include paths, cycles, and trees; routing problems associated with Euler and Hamilton; design of graphs realizing specified incidence conditions and other constraints. Attention directed toward problem solving, algorithms, and applications. One or more topics taken up in greater depth.

Prerequisite(s): Students may receive credit for EN.550.472/EN.553.472 or EN.553.672, but not both.;EN.553.291 OR EN.553.295 OR AS.110.201 OR AS.110.212

Corequisite(s): EN.550.171 may not be taken concurrently with EN.550.471 or EN.550.472

Area: Quantitative and Mathematical Sciences

EN.553.480. Numerical Linear Algebra. 4 Credits.

A course on computational linear algebra and applications. Topics include floating-point arithmetic algorithms and convergence Gaussian elimination for linear systems matrix decompositions (LU, Cholesky, QR) iterative methods for systems (Jacobi, Gauss Seidel) approximation of eigenvalues (power method, QR-algorithm) and also singular values and singular-value decomposition (SVD). Theoretical topics such as vector spaces, inner products norms, linear operators, matrix norms, eigenvalues and canonical forms of matrices (Jordan, Schur) are reviewed as needed. Matlab is used to solve all numerical exercises. Students who took EN.553.385 prior to Fall 2023 may not take EN.553.480.

Prerequisite(s): Students who took EN.553.385 prior to Fall 2023 may not take EN.553.480.:(EN.553.291 OR AS.110.201 OR AS.110.212) AND (AS.110.202 OR AS.110.211)

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.481. Numerical Analysis. 4 Credits.

Brief review of topics in elementary numerical analysis such as floating-point arithmetic, Gaussian elimination for linear equations, interpolation and approximation. Core topics to be covered: numerical linear algebra including eigenvalue and linear least-squares problems, iterative algorithms for nonlinear equations and least squares problems, and convergence theory of numerical methods. Other possible topics: sparse matrix computations, numerical solution of partial differential equations, finite element methods, and parallel algorithms.

Prerequisite(s): Students may take only one of EN.550.681, EN.553.481, EN.553.681 or EN.553.781.:(AS.110.202 OR AS.110.211) AND (EN.553.291 OR EN.553.295 OR AS.110.201 OR AS.110.212) AND (EN.553.291 OR AS.110.302 OR AS.110.417 OR EN.553.386 OR EN.553.388 OR EN.553.391)

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.488. Computing for Applied Mathematics. 3 Credits.

The aim of this course is to develop students' programming skills for solving problems commonly encountered in applied mathematics contexts. Specific problems that arise in applications of mathematics and data science (e.g. from finance, data analysis, or the physical sciences) are used to motivate concepts, techniques, and paradigms related to computation and programming. The Python language as well as a large collection of packages will be introduced. Students should be comfortable using computers but no prior programming background is required.

Prerequisite(s): Students may receive credit for EN.550.488/EN.553.488 or EN.553.688, but not both.;EN.553.310 OR EN.553.311 OR (EN.553.420 OR EN.553.421 AND (EN.553.430 OR EN.553.431))

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.491. Dynamical Systems. 4 Credits.

Mathematical concepts and methods for describing and analyzing linear and nonlinear systems that evolve over time. Topics include boundedness, stability of fixed points and attractors, feedback, optimality, Liapounov functions, bifurcation, chaos, and catastrophes. Examples drawn from population growth, economic behavior, physical and engineering systems. The main mathematical tools are linear algebra and basic differential equations.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.492. Mathematical Biology. 3 Credits.

This course will examine the mathematical methods relevant to modeling biological phenomena, particularly dynamical systems and probability.

Topics include ordinary differential equations and their simulation; stability and phase plane analysis; branching processes; Markov chains; and stochastically perturbed systems. Biological applications will be drawn from population growth, predator-prey dynamics, epidemiology, genetics, intracellular transport, and neuroscience.

Prerequisite(s): Students may receive credit for EN.553.492 or EN.553.692, but not both.;(EN.553.420 OR EN.553.421 OR EN.553.620) AND (AS.110.201 OR AS.110.212) AND (AS.110.302 OR AS.110.306 OR EN.553.291 OR EN.553.295)

Area: Natural Sciences, Quantitative and Mathematical Sciences

EN.553.493. Mathematical Image Analysis. 4 Credits.

This course gives an overview of various mathematical methods related to several problems encountered in image processing and analysis, and presents numerical schemes to address them. It will focus on problems like image denoising and deblurring, contrast enhancement, segmentation and registration. The different mathematical concepts shall be introduced during the course; they include in particular functional spaces such as Sobolev and BV, Fourier and wavelet transforms, as well as some notions from convex optimization and numerical analysis. Most of such methods will be illustrated with algorithms and simulations on discrete images, using MATLAB. Prerequisites : linear algebra, multivariate calculus, basic programming in MATLAB. Recommended Course Background: Real analysis

Prerequisite(s): Students may receive credit for EN.550.493/EN.553.493 or EN.553.693, but not both.;(AS.110.202 OR AS.110.211) AND (EN.553.291 OR EN.553.295 OR AS.110.201 OR AS.110.212)

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.494. Applied and Computational Multilinear Algebra. 3 Credits.

In this seminar we plan to discuss generalizations of theorems and algorithms from matrix theory to hypermatrices. More specifically the seminar will discuss hypermatrix/tensor algebras, rank, spectra and transforms. Using the python friendly free open-source mathematics software SageMath and the hypermatrix algebra package we will discuss applications of hypermatrices to combinatorics, machine learning and data analysis. Preliminary knowledge of the Python language is not required.

Prerequisite(s): Students may receive credit for EN.550.494/EN.553.494 or EN.553.694, but not both.;AS.110.201 OR AS.110.212 OR EN.553.291 OR EN.553.295

Area: Quantitative and Mathematical Sciences

EN.553.500. Undergraduate Research. 1 - 3 Credits.

Reading, research, or project work for undergraduate students. Pre-arranged individually between students and faculty.

Prerequisite(s): You must request Independent Academic Work using the Independent Academic Work form found in Student Self-Service: Registration, Online Forms.

EN.553.501. Senior Thesis. 3 Credits.

Prerequisite(s): You must request Independent Academic Work using the Independent Academic Work form found in Student Self-Service: Registration, Online Forms.

EN.553.502. Undergraduate Independent Study. 1 - 3 Credits.

Reading, research, or project work for undergraduate students. Pre-arranged individually between students and faculty. Recent topics and activities: percolation models, data analysis, course development assistance, and dynamical systems.

Prerequisite(s): You must request Independent Academic Work using the Independent Academic Work form found in Student Self-Service: Registration, Online Forms.

EN.553.506. Capstone Experience in Data Science. 3 - 6 Credits.

Project work for Data Science Master's students. Arranged individually between students and faculty.

Prerequisite(s): You must request Independent Academic Work using the Independent Academic Work form found in Student Self-Service: Registration, Online Forms.

Area: Quantitative and Mathematical Sciences

EN.553.512. Group Undergraduate Research. 1 - 3 Credits.

Reading, research, or project work for undergraduate students. Pre-arranged meetings between students and faculty. This section has a weekly research group meeting that students are expected to attend.

Prerequisite(s): You must request Independent Academic Work using the Independent Academic Work form found in Student Self-Service: Registration, Online Forms.

EN.553.552. Undergraduate Internship. 1 Credit.

Prerequisite(s): You must request Independent Academic Work using the Independent Academic Work form found in Student Self-Service: Registration, Online Forms.

EN.553.600. Mathematical Modeling and Consulting. 4 Credits.

Creating, analyzing and evaluating optimization and mathematical models using case studies. Project-oriented practice and guidance in modeling techniques, with emphasis on communication of methods and results. Applications may include transportation networks, scheduling, industrial processes, and telecommunications. Computation will be emphasized throughout using MATLAB. Recommend Course Background: EN.553.361 OR EN.553.362.

Prerequisite(s): Students may receive credit for EN.550.400/EN.553.400 or EN.553.600, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.601. Introduction to Research. 3 Credits.

This course will provide students with a comprehensive hands-on introduction to the research process, which includes performing a literature survey, mathematical modeling, theoretical, numerical, and/or empirical approaches while solving some of the problems in the research landscape. Some topics include (but are unlimited to) the following: • Systems Reliability Analysis • Systems Management • Network Analysis • Sports Scheduling • 5-G (and Next-Gen) Explorations • Mechanical Ventilation Data Analysis and Management In the process, students will have the experience to produce their status reports and results orally and in writing where the goal is to provide an initial working publication that can be extended for upcoming conference and/or journal submissions.

Area: Quantitative and Mathematical Sciences

EN.553.602. Research and Design in Applied Mathematics: Data Mining. 4 Credits.

The course will be project oriented with focus on practical uses of machine learning and data mining. Throughout the semester, teams of 4 will work on topics decided by the students and the instructor.

Prerequisite(s): EN.553.636

Area: Quantitative and Mathematical Sciences

EN.553.613. Applied Statistics and Data Analysis. 4 Credits.

An introduction to basic concepts, techniques, and major computer software packages in applied statistics and data analysis. Topics include numerical descriptive statistics, observations and variables, sampling distributions, statistical inference, linear regression, multiple regression, design of experiments, nonparametric methods, and sample surveys. Real-life data sets are used in lectures and computer assignments. Intensive use of statistical packages such as R to analyze data. Recommended Course Background: EN.553.112 or EN.553.310 or EN.553.311 or EN.553.420.

Prerequisite(s): Students may receive credit for EN.550.413/EN.553.413 or EN.553.613, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.614. Applied Statistics and Data Analysis II. 3 Credits.

Part II of a sequence on data analysis and linear models. Topics include categorical and discrete data analysis, mixed models, semiparametric and nonparametric regression, and generalized additive models. Applications of these methods using the R environment for statistical computing will be emphasized.

Prerequisite(s): Students may receive credit for EN.550.414/EN.553.414 or EN.553.614, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.620. Probability. 4 Credits.

Probability and its applications, at the calculus level. Emphasis on techniques of application and on rigorous mathematical demonstration. Probability, combinatorial probability, random variables, distribution functions, important probability distributions, independence, conditional probability, moments, covariance and correlation, limit theorems. Recommended course background: (AS.110.109 or AS.110.113) and previously or concurrently (AS.110.202 or AS.110.201 or AS.110.212).

Prerequisite(s): Students may receive credit for only one of the following: EN.553.420 OR EN.553.421 OR EN.553.620.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.626. Introduction to Stochastic Processes. 4 Credits.

Mathematical theory of stochastic processes. Emphasis on deriving the dependence relations, statistical properties, and sample path behavior including random walks, Markov chains (both discrete and continuous time), Poisson processes, martingales, and Brownian motion. Applications that illuminate the theory. Students may receive credit for EN.553.426 or EN.553.626. Recommended course background: (EN.553.291 OR AS.110.201 OR AS.110.212).

Prerequisite(s): EN.553.620; Students may receive credit for EN.550.426/ EN.553.426 or EN.553.626, but not both.

Corequisite(s): Students may not enroll in EN.553.620 in the same semester.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.627. Stochastic Processes and Applications to Finance. 4 Credits.

A development of stochastic processes with substantial emphasis on the processes, concepts, and methods useful in mathematical finance. Relevant concepts from probability theory, particularly conditional probability and conditional expectation, will be briefly reviewed. Important concepts in stochastic processes will be introduced in the simpler setting of discrete-time processes, including random walks, Markov chains, and discrete-time martingales, then used to motivate more advanced material. Most of the course will concentrate on continuous-time stochastic processes, particularly martingales, Brownian motion, diffusions, and basic tools of stochastic calculus. Examples will focus on applications in finance, economics, business, and actuarial science. Recommended Course Background: EN.553.620.

Prerequisite(s): Students may receive credit for only one of EN.550.427, EN.553.427, EN.553.627

Area: Quantitative and Mathematical Sciences

EN.553.628. Stochastic Processes and Applications to Finance II. 4 Credits.

A basic knowledge of stochastic calculus and Brownian motion is assumed. Topics include stochastic differential equations, the Feynman-Kac formula and connections to partial differential equations, changes of measure, fundamental theorems of asset pricing, martingale representations, first passage times and pricing of path-dependent options, and jump processes.

Prerequisite(s): Students may receive credit for EN.550.428/EN.553.428 or EN.553.628, but not both.

Area: Quantitative and Mathematical Sciences

EN.553.630. Mathematical Statistics. 4 Credits.

Introduction to the basic principles of mathematical statistics and data analysis. Emphasis on techniques of application. Classical parametric estimation, hypothesis testing, and multiple decision problems; linear models, analysis of variance, and regression; nonparametric and robust procedures; decision-theoretic setting, Bayesian methods. Recommended Course Background: EN.553.620 AND (AS.110.201 OR AS.110.212 OR EN.553.291).

Prerequisite(s): Students may receive credit for EN.550.430/EN.553.430 or EN.553.630, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.632. Bayesian Statistics. 3 Credits.

The course will cover Bayesian methods for exploratory data analysis. The emphasis will be on applied data analysis in various disciplines. We will consider a variety of topics, including introduction to Bayesian inference, prior and posterior distribution, hierarchical models, spatial models, longitudinal models, models for categorical data and missing data, model checking and selection, computational methods by Markov Chain Monte Carlo using R or Matlab. We will also cover some nonparametric Bayesian models if time allows, such as Gaussian processes and Dirichlet processes. Recommended prerequisites: EN.553.620 and (EN.553.630 or EN.553.730)

Prerequisite(s): Students may take only one of EN.550.632, EN.553.432, EN.553.632 or EN.553.732.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.633. Monte Carlo Methods. 4 Credits.

The objective of the course is to survey essential simulation techniques for popular stochastic models. The stochastic models may include classical time-series models, Markov chains and diffusion models. The basic simulation techniques covered will be useful in sample-generation of random variables, vectors and stochastic processes, and as advanced techniques, importance sampling, particle filtering and Bayesian computation may be discussed. Recommended Course Background: EN.553.630.

Prerequisite(s): Students may receive credit for EN.550.433/EN.553.433 or EN.553.633, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.636. Introduction to Data Science. 4 Credits.

Today the term Data Science is widely used covering a broad range of topics from mathematics and algorithms to actual data analysis and machine learning techniques. This course provides a thorough survey of relevant methods balancing the theory and the application aspects. Accordingly, the material and the discussions alternate between the methodology along with its underlying assumptions and the implementations along with their applications. We will cover several supervised methods for regression and classification, as well as unsupervised methods for clustering and dimensional reduction. To name a few in chronological order, the topics will include generalized linear regression, principal component analysis, nearest neighbor and Bayesian classifiers, support vector machines, logistic regression, decision trees, random forests, K-means clustering, Gaussian mixtures and Laplacian eigenmaps. The course uses Python and Jupyter Notebook and includes visualization techniques throughout the semester. Time permitting, an introduction to the Structured Query Language (SQL) is provided toward the end of the semester.

Prerequisite(s): Students may receive credit for EN.550.436/EN.553.436 or EN.553.636, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.639. Time Series Analysis. 3 Credits.

Time series analysis from the frequency and time domain approaches. Descriptive techniques; regression analysis; trends, smoothing, prediction; linear systems; serial correlation; stationary processes; spectral analysis. Recommended course background: EN.553.620 and (AS.110.201 OR AS.110.212 OR EN.553.291)

Prerequisite(s): Students may receive credit for EN.550.439/EN.553.439 or EN.553.639, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.641. Equity Markets and Quantitative Trading. 3 Credits.

This course introduces equity markets from a mathematical point of view. The properties of equities and equity-linked instruments will be described. Several quantitative trading strategies will be studied. Order execution tactics and the effect of market structure will be analyzed. Students will select a specialized aspect of the equity markets to investigate and complete a related independent project.

Prerequisite(s): Students may receive credit for EN.550.441/EN.553.441 or EN.553.641, but not both.;EN.553.442 or EN.553.642, or instructor's permission

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.642. Investment Science. 4 Credits.

This course offers a rigorous treatment of the subject of investment as a scientific discipline. Mathematics is employed as the main tool to convey the principles of investment science and their use to make investment calculations for good decision-making. Topics covered in the course include the basic theory of interest and its application to fixed-income securities, cash flow analysis and capital budgeting, mean-variance portfolio theory, and the associated capital asset pricing model, utility function theory and risk analysis, derivative securities and basic option theory, portfolio evaluation. The student is expected to be comfortable with the use of mathematics as a method of deduction and problem solving. Recommended Course Background: (AS.110.109 OR AS.110.113) AND (EN.553.291 OR AS.110.201 OR AS.110.212) AND (EN.553.310 OR EN.553.311 OR EN.553.420 OR EN.553.430).

Prerequisite(s): Students may receive credit for EN.550.342 or EN.550.442/EN.553.442 or EN.553.642, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.643. Energy Markets and Risk Management. 3 Credits.

The course objectives are to provide a deep understanding of commodities markets, with a focus on Energy (Natural Gas, Electricity, Renewable Energy, Crude Oil) and extension to clean energy and corresponding carbon emission markets. The important instruments (Forward, Futures, Options) will be redefined, valued and used in real risk management examples. This course provides an opportunity to bridge the gap between financial models in academy and risk management solutions in complicated energy markets. Students should have a background in probability and financial derivatives.

Area: Quantitative and Mathematical Sciences

EN.553.644. Introduction to Financial Derivatives. 4 Credits.

This course will develop the mathematical concepts and techniques for modeling cash instruments and their hybrids and derivatives. Prerequisites: background in Probability and Financial Derivatives.

Prerequisite(s): Students may receive credit for EN.550.444/ EN.553.444 or EN.553.644, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.645. Interest Rate and Credit Derivatives. 4 Credits.

Advances in corporate finance, investment practice and the capital markets have been driven by the development of a mathematically rigorous theory for financial instruments and the markets in which they trade. This course builds on the concepts, techniques, instruments and markets introduced in EN.553.644. In addition to new topics in credit enhancement and structured securities, the focus is expanded to include applications in portfolio theory and risk management, and covers some numerical and computational approaches. Recommended Course Background: EN.553.644

Prerequisite(s): Students may receive credit for EN.550.445/EN.553.445 or EN.553.645, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.646. Risk Measurement/Management in Financial Markets. 4 Credits.

This course applies advanced mathematical techniques to the measurement, analysis, and management of risk. The focus is on financial risk. Sources of risk for financial instruments (e.g., market risk, interest rate risk, credit risk) are analyzed; models for these risk factors are studied and the limitation, shortcomings and compensatory techniques are addressed. Recommended Course Background: EN.553.644.

Prerequisite(s): Students may receive credit for EN.550.446/EN.553.446 or EN.553.646, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.647. Quantitative Portfolio Theory and Performance Analysis. 4 Credits.

This course focuses on modern quantitative portfolio theory, models, and analysis. Topics include intertemporal approaches to modeling and optimizing asset selection and asset allocation; benchmarks (indexes), performance assessment (including, Sharpe, Treynor and Jensen ratios) and performance attribution; immunization theorems; alpha-beta separation in management, performance measurement and attribution; Replicating Benchmark Index (RBI) strategies using cash securities / derivatives; Liability-Driven Investment (LDI); and the taxonomy and techniques of strategies for traditional management: Passive, Quasi-Passive (Indexing) Semi-Active (Immunization & Dedicated) Active (Scenario, Relative Value, Total Return and Optimization). In addition, risk management and hedging techniques are also addressed.

Prerequisite(s): Students may receive credit for (EN.550.447 OR EN.553.447) OR EN.553.647, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.648. Financial Engineering and Structured Products. 4 Credits.

This course focuses on structured securities and the structuring of aggregates of financial instruments into engineered solutions of problems in capital finance. Topics include the fundamentals of creating asset-backed and structured securities—including mortgage-backed securities (MBS), stripped securities, collateralized mortgage obligations (CMOs), and other asset-backed collateralized debt obligations (CDOs)—structuring and allocating cash-flows as well as enhancing credit; equity hybrids and convertible instruments; asset swaps, credit derivatives and total return swaps; assessment of structure-risk interest rate-risk and credit-risk as well as strategies for hedging these exposures; managing portfolios of structured securities; and relative value analysis (including OAS and scenario analysis).

Prerequisite(s): Students may receive credit for EN.550.448/EN.553.448 or EN.553.648, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.649. Advanced Equity Derivatives. 4 Credits.

This course will cover the pricing, trading and risk management of equity derivatives, with emphasis on more exotic derivatives such as path-dependent and multi-asset derivatives. The course will emphasize practical issues: students will build their own pricing and risk management tools, and gain experience simulating the dynamic hedging of a complex derivatives portfolio. Students will practice structuring and selling equity derivative products. Pricing issues such as model selection, unobservable input parameters and calibration will be discussed, and students will learn techniques to manage the often highly nonlinear and discontinuous risks associated with these products. The course will have a significant computing component: both in the classroom and as homework projects, students will use Excel, write VBA macros and write and call C++ routines in the Microsoft Windows environment (which is the most common computing environment used by the financial industry).

Recommended Course Background: EN.553.444.

Prerequisite(s): Students may receive credit for EN.550.449/EN.553.449 or EN.553.649, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.650. Computational Molecular Medicine. 4 Credits.

Computational systems biology has emerged as the dominant framework for analyzing high-dimensional “omics” data in order to uncover the relationships among molecules, networks and disease. In particular, many of the core methodologies are based on statistical modeling, including machine learning, stochastic processes and statistical inference. We will cover the key aspects of this methodology, including measuring associations, testing multiple hypotheses, and learning predictors, Markov chains and graphical models. In addition, by studying recent important articles in cancer systems biology, we will illustrate how this approach enhances our ability to annotate genomes, discover molecular disease networks, detect disease, predict clinical outcomes, and characterize disease progression. Whereas a good foundation in probability and statistics is necessary, no prior exposure to molecular biology is required (although helpful). Recommended Course Background: EN.553.620 AND EN.553.630.

Prerequisite(s): Students may receive credit for EN.550.450/EN.553.450 or EN.553.650, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.653. Mathematical Game Theory. 4 Credits.

Mathematical analysis of cooperative and noncooperative games. Theory and solution methods for matrix game (two players, zero-sum payoffs, finite strategy sets), games with a continuum of strategies, N-player games, games in rule-defined form. The roles of information and memory. Selected applications to economic, recreational, and military situations. Prereq: Multivariable Calculus, probability, linear algebra. Recommended Course Background: (AS.110.202 OR AS.110.211) AND EN.553.620 AND (EN.553.291 OR AS.110.201 OR AS.110.212)

Prerequisite(s): Students may receive credit for EN.550.453/EN.553.453 or EN.553.653, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.661. Optimization in Finance. 4 Credits.

A survey of many of the more important optimization methods and tools that are found to be useful in financial applications. Recommended Course Background: EN.553.642 OR EN.553.644.

Prerequisite(s): Students may receive credit for EN.550.461/EN.553.461 or EN.553.661, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.662. Optimization for Data Science. 3 Credits.

The course provides foundations and algorithms addressing optimization problems in modern data science. It covers smooth unconstrained descent methods (including deterministic and stochastic gradient), smooth constrained optimization and some non-smooth situations in the convex case. Each of these optimization problems will be related to specific data science training algorithms (such as logistic regression, neural networks, support vector machines or lasso). Prerequisites include multivariable calculus and linear algebra. Homework will include some programming components and students will be expected to have basic proficiency in computer languages such as Python (preferred) or Matlab. Recommended Course Background: Multivariable Calculus and Linear algebra.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.663. Network Models in Operations Research. 4 Credits.

In-depth mathematical study of network flow models in operations research, with emphasis on combinatorial approaches for solving them. Introduction to techniques for constructing efficient algorithms, and to some related data structures, used in solving shortest-path, maximum-volume, flow, and minimum-cost flow problems. Emphasis on linear models and flows, with brief discussion of non-linear models and network design. Recommended Course Background: EN.553.361 OR EN.553.761 OR EN.553.661.

Prerequisite(s): Students may receive credit for EN.550.463/EN.553.463 or EN.553.663, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.665. Introduction to Convexity. 4 Credits.

Convexity is a simple mathematical concept that has become central in a diverse range of applications in engineering, science and business applications. Our main focus from the applications perspective will be the use of convexity within optimization problems, where convexity plays a key role in identifying the "easy" problems from the "hard" ones. The course will have an equal emphasis on exposing the rich mathematical structure of the field itself (properties of convex sets, convex functions, Helly-Caratheodory-Radon type theorems, polarity/duality, subdifferential calculus, polyhedral theory), and demonstrating how these ideas can be leveraged to model and solve optimization problems (via a detailed study of linear programming and basics of nonlinear convex optimization). Recommend Course Background: Familiarity with basic real analysis, linear algebra.

Prerequisite(s): Students may receive credit for EN.550.465 /EN.553.465 or EN.553.665, but not both.

EN.553.667. Deep Learning in Discrete Optimization. 3 Credits.

The goal of the course is to examine research-level topics in the application of deep-learning techniques to the solution of computational problems in discrete optimization. The first part of the course will cover background material, introducing students to deep learning (focusing on practical aspects) and covering major topics in computational discrete optimization: heuristic methods, dynamic programming, linear programming, cutting planes, column generation, and branch-and-bound. We will then make an in-depth study of research papers where deep learning has been proposed as a solution-technique in discrete optimization, aiming towards discussions of open research questions. Prerequisites: General mathematical maturity is expected: students should feel comfortable reading on their own Part 1 (Applied Math and Machine Learning Basics) in the text Deep Learning by Goodfellow, Bengio, and Courville.

EN.553.669. Large-Scale Optimization For Data Science. 3 Credits.

Optimization formulations and algorithms have long played a central role in data analysis and machine learning. In the era of big data, the need to solve large-scale optimization problems is ubiquitous in essentially all quantitative areas of human endeavor, including industry and science. This course is a mathematically rigorous and comprehensive introduction to the field of large-scale optimization for data science and machine learning, and is based on the latest results and insights. We discuss the most important algorithms in the area, with analysis of their convergence and complexity properties, as well as their practical implementations. Applications of the methods covered in the course can be found virtually in all fields of data science including text analysis, page ranking, speech recognition, image classification, finance and decision sciences.

Prerequisites: background in Linear Algebra (or Computational Linear Algebra), Multivariable Calculus, Probability, and a basic knowledge of programming - experience with at least one high-level computing language (e.g.: Python, Matlab, Julia, C, ...).

Area: Quantitative and Mathematical Sciences

EN.553.671. Combinatorial Analysis. 4 Credits.

An introduction to combinatorial analysis at the graduate level. Meets concurrently with 553.471. Counting techniques: generating functions, recurrence relations, Polya's theorem. Combinatorial designs: Latin squares, finite geometries, balanced incomplete block designs. Emphasis on problem solving. Recommended Course Background: EN.553.291 or AS.110.201

Prerequisite(s): Students may receive credit for EN.550.471/EN.553.471 or EN.553.671, but not both.

EN.553.672. Graph Theory. 4 Credits.

Study of systems of "vertices" with some pairs joined by "edges." Theory of adjacency, connectivity, traversability, feedback, and other concepts underlying properties important in engineering and the sciences. Topics include paths, cycles, and trees; routing problems associated with Euler and Hamilton; design of graphs realizing specified incidence conditions and other constraints. Attention directed toward problem solving, algorithms, and applications. One or more topics taken up in greater depth. Recommended Course Background: (EN.553.291 OR AS.110.201 OR AS.110.212)

Prerequisite(s): Students may receive credit for EN.550.472/EN.553.472 or EN.553.672, but not both.

EN.553.680. Numerical Linear Algebra. 4 Credits.

A course on computational linear algebra and applications. Topics include floating-point arithmetic algorithms and convergence Gaussian elimination for linear systems matrix decompositions (LU, Cholesky, QR) iterative methods for systems (Jacobi, Gauss Seidel) approximation of eigenvalues (power method, QR-algorithm) and also singular values and singular-value decomposition (SVD). Theoretical topics such as vector spaces, inner products norms, linear operators, matrix norms, eigenvalues and canonical forms of matrices (Jordan, Schur) are reviewed as needed. Matlab is used to solve all numerical exercises.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.681. Numerical Analysis. 4 Credits.

Brief review of topics in elementary numerical analysis such as floating-point arithmetic, Gaussian elimination for linear equations, interpolation and approximation. Core topics to be covered: numerical linear algebra including eigenvalue and linear least-squares problems, iterative algorithms for nonlinear equations and least squares problems, and convergence theory of numerical methods. Other possible topics: sparse matrix computations, numerical solution of partial differential equations, finite element methods, and parallel algorithms. Recommended Course Background: Multivariable calculus, linear algebra, and differential equations.

Prerequisite(s): Students may take only one of EN.550.681, EN.553.481, EN.553.681 or EN.553.781.

EN.553.688. Computing for Applied Mathematics. 3 Credits.

The aim of this course is to develop students' programming skills for solving problems commonly encountered in applied mathematics contexts. Specific problems that arise in applications of mathematics and data science (e.g. from finance, data analysis, or the physical sciences) are used to motivate concepts, techniques, and paradigms related to computation and programming. The Python language as well as a large collection of packages will be introduced. Recommended Course Background: EN.553.310 OR EN.553.311 OR (EN.553.420 AND EN.553.430). Students should be comfortable using computers but no prior programming background is required.

Prerequisite(s): Students may receive credit for EN.553.488 or EN.553.688, but not both.

EN.553.691. Dynamical Systems. 4 Credits.

Mathematical concepts and methods for describing and analyzing linear and nonlinear systems that evolve over time. Topics include boundedness, stability of fixed points and attractors, feedback, optimality, Liapounov functions, bifurcation, chaos, and catastrophes. Examples drawn from population growth, economic behavior, physical and engineering systems. The main mathematical tools are linear algebra and basic differential equations.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.692. Mathematical Biology. 3 Credits.

This course will examine the mathematical methods relevant to modeling biological phenomena, particularly dynamical systems and probability. Topics include ordinary differential equations and their simulation; stability and phase plane analysis; branching processes; Markov chains; and stochastically perturbed systems. Biological applications will be drawn from population growth, predator-prey dynamics, epidemiology, genetics, intracellular transport, and neuroscience. Recommended Course Background: EN.553.620 AND (AS.110.201 OR AS.110.212) AND (AS.110.302 OR AS.110.306 OR EN.553.291)

Prerequisite(s): Students may receive credit for EN.550.492/EN.553.492 or EN.553.692, but not both.

Area: Natural Sciences, Quantitative and Mathematical Sciences

EN.553.693. Mathematical Image Analysis. 4 Credits.

This course gives an overview of various mathematical methods related to several problems encountered in image processing and analysis, and presents numerical schemes to address them. It will focus on problems like image denoising and deblurring, contrast enhancement, segmentation and registration. The different mathematical concepts shall be introduced during the course; they include in particular functional spaces such as Sobolev and BV, Fourier and wavelet transforms, as well as some notions from convex optimization and numerical analysis. Most of such methods will be illustrated with algorithms and simulations on discrete images, using MATLAB. Prerequisites : linear algebra, multivariate calculus, basic programming in MATLAB. Recommended Course Background: A solid foundation Multivariable Calculus, Linear Algebra, and Probability. Real Analysis may help too, but it is not necessary.

Prerequisite(s): Students may receive credit for EN.550.493/EN.553.493 or EN.553.693, but not both.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.694. Applied and Computational Multilinear Algebra. 3 Credits.

In this seminar we plan to discuss generalizations of theorems and algorithms from matrix theory to hypermatrices. More specifically the seminar will discuss hypermatrix/tensor algebras, rank, spectra and transforms. Using the python friendly free open-source mathematics software SageMath and the hypermatrix algebra package we will discuss applications of hypermatrices to combinatorics, machine learning and data analysis. Preliminary knowledge of the Python language is not required. Recommended Course Background: AS.110.212 OR AS.110.201 OR EN.553.291.

Prerequisite(s): Students may receive credit for EN.553.494 or EN.553.694, but not both.

EN.553.701. Real Analysis: Preparation for the Ph.D. Introductory Examination. 4 Credits.

This course is designed to prepare students for the Real Analysis part of the introductory exam of the Department of Applied Mathematics and Statistics. In this course we will cover fundamental topics in real analysis, such as, Set Theory, The Topology of Euclidean Space, Continuous Mappings, Uniform Convergence, Differentiable Mappings, Inverse & Implicit Function Theorems, Integration Theory, Fourier Series, and Basics of Differential Equations.

EN.553.720. Probability Theory I. 4 Credits.

The course objectives are to develop probabilistic reasoning and problem solving approaches, to provide a rigorous mathematical basis for probability theory, and to examine several important results in the theory of probability. Topics include axiomatic probability, independence, random variables and their distributions, expectation, integration, variance and moments, probability inequalities, and modes of convergence of random variables. The course will include introductory measure theory as needed. Students are expected to have previous study of both analysis and probability. This course is the first half of a yearlong sequence. The second semester's course, EN.553.721 Probability Theory II, will cover classical limit theorems, characteristic functions, and conditional expectation. Prerequisite: real analysis (AS.110.405/ AS.110.415)

Prerequisite(s): Students may take EN.550.620 or EN.553.720, but not both.

EN.553.721. Probability Theory II. 3 Credits.

Probability at the level of measure theory, focusing on limit theory. Modes of convergence, Poisson convergence, three-series theorem, strong law of large numbers, continuity theorem, central limit theory, Berry-Esseen theorem, infinitely divisible and stable laws. Recommended Course Background: EN.553.720 AND (AS.110.405 OR AS.110.415)

EN.553.728. Optimal Transport. 3 Credits.

This course is designed to cover recent results in Optimal Transport from an applied mathematical perspective. We will briefly start by covering the mathematical formulations required to understand basic applications during the first few weeks, but the majority of the class will consist of reading and presenting papers in the student's fields of interest that have significant overlap with Optimal Transport, both theoretical and applied. Faculty from JHU (and possibly other institutions) will occasionally present on how OT features in their research as well. Among other topics, we will focus on applications to Manifold Learning. The structure of this class is modeled after Equivariant Machine Learning (EN.553.743.01.FA22).

EN.553.729. Topics in Probability. 3 Credits.

This seminar course will discuss the "probabilistic method," with applications to random graphs and percolation theory. Topics include linearity of expectation, first and second moment methods, the local lemma, correlation inequalities, martingale concentration results, the evolution of random graphs, Poisson approximation, stochastic ordering, bond and site percolation models, and the substitution method for bounding percolation thresholds. Students will present at least two short talks on relevant topics or applications of their choice. Prerequisites: 553.620 Introduction to Probability and 553.672 Graph Theory, or equivalents. No auditors permitted.

EN.553.730. Statistical Theory. 4 Credits.

The fundamentals of mathematical statistics will be covered. Topics include: distribution theory for statistics of normal samples, exponential statistical models, the sufficiency principle, least squares estimation, maximum likelihood estimation, uniform minimum variance unbiased estimation, hypothesis testing, the Neyman-Pearson lemma, likelihood ratio procedures, the general linear model, the Gauss-Markov theorem, simultaneous inference, decision theory, Bayes and minimax procedures, chi-square methods, goodness-of-fit tests, and nonparametric and robust methods.

Prerequisite(s): Students may take EN.550.630 or EN.553.730, but not both.

EN.553.731. Statistical Theory II. 3 Credits.

Advanced concepts and tools fundamental to research in mathematical statistics and statistical inference: asymptotic theory; optimality; various mathematical foundations.

Prerequisite(s): EN.553.730 OR EN.553.720 OR (AS.110.405 AND EN.553.430) Knowledge of real analysis is required.

EN.553.733. Nonparametric Bayesian Statistics. 3 Credits.

This course covers advanced topics in Bayesian statistical analysis beyond the introductory course. Therefore knowledge of basic Bayesian statistics is assumed (at the level of "A first course in Bayesian statistical methods", by Peter Hoff (Springer, 2009). The models and computational methods will be introduced with emphasis on applications to real data problems. This course will cover nonparametric Bayesian models including Gaussian process, Dirichlet process (DP), Polya trees, dependent DP, Indian buffet process, etc. Recommended Course Background: EN.553.432 or EN.553.632 or EN.553.732 or permission from the instructor

EN.553.735. Topics in Statistical Pattern Recognition. 3 Credits.

The Dissimilarity Representation for Pattern Recognition. This course will investigate aspects of statistical inference and statistical pattern recognition associated with observing only dissimilarities between entities rather than observing feature vectors associated with the individual entities themselves.

EN.553.736. System Identification and Likelihood Methods. 2 Credits.

The focus of this roundtable-format course will be stochastic modeling as relates to system identification and maximum likelihood. The principles and algorithms being covered in this course have tremendous importance in the world at large. For example, maximum likelihood is arguably the most popular method for parameter estimation in most real-world applications. System identification is the term used in many fields to refer to the process of mathematical model building from experimental data, with a special focus on dynamical systems. The system identification process refers to several important aspects of model building, including selection of the model form (linear or nonlinear, static or dynamic, etc.), experimental design, parameter estimation, and model validation. This course will cover topics such as the maximum likelihood formulation and theory for dynamical systems, the EM (expectation-maximization) algorithm and its variants, Fisher information, common model structures, online versus offline estimation, the role of feedback in identification (i.e., open-loop versus closed-loop estimation), standard and extended Kalman filtering, and uncertainty characterization (e.g., confidence regions). Recommended Course Background: Undergraduate-level matrix theory and ordinary differential equations; graduate-level course in probability and statistics (e.g., 553.430 or equivalent; in particular, students should have prior exposure to maximum likelihood and Bayes' rule). Prior experience in data analysis and algorithms will be helpful.

EN.553.738. High-Dimensional Approximation, Probability, and Statistical Learning. 3 Credits.

The course covers fundamental mathematical ideas for certain approximation and statistical learning problems in high dimensions. We start with basic approximation theory in low-dimensions, in particular linear and nonlinear approximation by Fourier and wavelets in classical smoothness spaces, and discuss applications in imaging, inverse problems and PDE's. We then introduce notions of complexity of function spaces, which will be important in statistical learning. We then move to basic problems in statistical learning, such as regression and density estimation. The interplay between randomness and approximation theory is introduced, as well as fundamental tools such as concentration inequalities, basic random matrix theory, and various estimators are constructed in detail, in particular multi scale estimators. At all times we consider the geometric aspects and interpretations, and will discuss concentration of measure phenomena, embedding of metric spaces, optimal transportation distances, and their applications to problems in machine learning such as manifold learning and dictionary learning for signal processing.

EN.553.739. Statistical Pattern Recognition Theory & Methods. 3 Credits.

This biennial course covers topics in the theory, methods, and applications of machine learning from an explicitly statistical perspective. Recommended Course Background: (EN.550.420 OR EN.553.420 OR EN.553.620) AND (EN.550.430 OR EN.553.430 OR EN.553.630)

EN.553.740. Machine Learning I. 3 Credits.

This course is the first part of a two-semester sequence that focuses on theoretical and practical aspects of statistical learning. After introducing background material on inner-product spaces, reproducing kernels and on optimization, the course discusses fundamental concepts of machine learning (such as generalization error, Bayes estimators and the bias vs. variance dilemma) and studies a collection of learning algorithms for classification and regression. The topics that are discussed include linear and kernel regression, support vector machines, lasso, logistic regression, decision trees and neural networks. Students will need a solid background in multivariate calculus, linear algebra, probability and statistics to complete the course. Recommended Course background: 553.620 and 553.630 or higher, and prerequisites for these courses.

EN.553.741. Machine Learning II. 3 Credits.

This course is the second part of a two-semester sequence that focuses on theoretical and practical aspects of statistical learning. The course will have two distinct parts. The first one will discuss some fundamentals of statistical learning theory, including some concentration inequality, generalization bounds and VC dimension. The second one will introduce problems and algorithms for unsupervised data analysis, including dimension reduction, manifold learning and clustering. Recommended course background: 553.740.

EN.553.742. Statistical Inference on Graphs. 3 Credits.

This course provides an introduction to and overview of current research in random graph inference, with a particular focus on spectral methods and their applications to inference for independent-edge random graphs. Topics include concentration inequalities; analysis of matrix perturbations; spectral decompositions of graph adjacency and Laplacian matrices; consistent estimation of latent variables associated to vertices; clustering, community detection, and classification in networks; and multi-sample hypothesis testing for graphs. Emphasis will be on a framework for establishing classical properties—consistency, normality, and efficiency—for estimators of graph parameters. Students will read papers in the literature and are expected to participate actively in class. Recommended prerequisites EN.553.792 and EN.553.630.

EN.553.743. Equivariant Machine Learning. 3 Credits.

This is a graduate course in the topic of equivariant machine learning and graph neural networks. The course will have a fixed schedule with a preselected list of theoretical research papers to discuss each class (2.5 hours once a week). Each week two students will present one paper to the class and discussion will follow. The evaluation will be based on the quality and clarity of the presentations and in-class participation. There will be no homework nor exams. Prerequisites include basic knowledge of machine learning and probability.

EN.553.749. Advanced Financial Theory. 4 Credits.

The first part of the course will review in depth the main instruments in the various asset classes, as well as the founding results on investment decision, capital budgeting and project financing. The second part will analyze the theory of the firm: capital structure, dilution and share repurchase, dividend policy, Modigliani-Miller theorem and will lead to the contingent claim pricing of corporate debt and equity as in Merton (1974) and its extensions. The third part will extend the CAPM to the Arbitrage Pricing Theory of Ross (1976) and its theoretical and operational consequences. The fourth part will be dedicated to the stochastic modelling of the yield curve to price caps, floors and swaptions, and their use in the Asset Liability Management of a bank and insurance company. This course will not begin until mid-October.

EN.553.753. Commodity Markets and Green Energy Finance. 4 Credits.

Energy markets and energy derivatives are unique and require special attention and special risk management tools. Part I (R. Galeeva): The overview of important fundamental of the core markets: crude oil and refined products, natural gas and electricity; statistical study of the "stylized" facts about commodities prices. Basic evaluation of Commonly traded energy instruments: forwards, swaps, spreads. Forward yields, forward curve structure, carry formalism, using rolling contracts, risk neutral evaluation; BS evaluation with time dependent volatility. Forward dynamics, term structure of volatility and correlations. Samuelson effect, behavior of correlations. Detailed evaluation of typical commodity derivatives: swaption and spread option, including the calibration to the market data and the calculation of sensitivities, Greeks. Applications of spread options to commodity assets evaluation, such as power plant, storage, pipelines. The emphasis will be on the practical experience of building the pricing and hedging models for Energy Derivatives. The work will involve Excel and programming in Python (or any other language). Part II (taught by Dr. H. Geman). Topics include: Shipping Markets, Freight Indexes, Forward Freight Agreements, and Supply Chain. Coal markets across the world and their Rebirth Metal physical markets, major Exchanges (LME, SHFE), and the role of Metals in the development of Renewables, particularly Steel, Aluminum, Palladium. Agricultural (grains and softs) markets, Biofuels, fertilizers and water. Examples of forward curves and their different shapes; examples of volatility skews. Relationship between price volatility and Inventory; Theory of Storage Usefulness of Asian options in Commodities and Valuation. Commodity Indexes and the Different Ways of Investing in Commodities"

EN.553.761. Nonlinear Optimization I. 3 Credits.

This course considers algorithms for solving various nonlinear optimization problems and, in parallel, develops the supporting theory. The primary focus will be on unconstrained optimization problems. Topics for the course will include: necessary and sufficient optimality conditions; steepest descent method; Newton and quasi-Newton based line-search, trust-region, and adaptive cubic regularization methods; linear and nonlinear least-squares problems; linear and nonlinear conjugate gradient methods. Recommended Course Background: Multivariable Calculus, Linear Algebra, Real Analysis such as AS.110.405
Prerequisite(s): Students may take EN.550.661 or EN.553.761, but not both.

EN.553.762. Nonlinear Optimization II. 3 Credits.

This course considers algorithms for solving various nonlinear optimization problems and, in parallel, develops the supporting theory. The primary focus will be on constrained optimization problems. Topics for the course will include: necessary and sufficient optimality conditions for constrained optimization; projected-gradient and two-phase accelerated subspace methods for bound-constrained optimization; simplex and interior-point methods for linear programming; duality theory; and penalty, augmented Lagrangian, sequential quadratic programming, and interior-point methods for general nonlinear programming. In addition, we will consider the Alternating Direction Method of Multipliers (ADMM), which is applicable to a huge range of problems including sparse inverse covariance estimation, consensus, and compressed sensing. Recommended Course Background: Multivariable Calculus, Linear Algebra, Real Analysis such as AS.110.405.

EN.553.763. Stochastic Search & Optimization. 3 Credits.

An introduction to stochastic search and optimization, including discrete and continuous optimization problems. Topics will include the “no free lunch” theorems, beneficial effects of injected Monte Carlo randomness, algorithms for global and local optimization problems, random search, recursive least squares, stochastic approximation, simulated annealing, evolutionary and genetic algorithms, and statistical multiple comparisons. Recommended Course Background: Graduate course in probability and statistics and knowledge of basic matrix algebra.

EN.553.764. Modeling, Simulation, and Monte Carlo. 3 Credits.

Concepts and statistical techniques critical to constructing and analyzing effective simulations; emphasis on generic principles rather than specific applications. Topics include model building (bias-variance tradeoff, model selection, Fisher information), benefits and drawbacks of simulation modeling, random number generation, simulation-based optimization, discrete multiple comparisons using simulations, Markov chain Monte Carlo (MCMC), and input selection using optimal experimental design.

EN.553.766. Combinatorial Optimization. 3 Credits.

The main goal of this course is to introduce students to combinatorial optimization techniques. The first part of the course will focus on combinatorial algorithms for classical problems. The next part of the course will show how polyhedral theory can be used to deal with combinatorial optimization problems in a unifying manner. Familiarity with linear programming and algorithms desirable but not strictly required. Recommended Course Background: Linear Algebra.

EN.553.767. Iterative Algorithms in Machine Learning: Theory and Applications. 3 Credits.

This course teaches an overview of modern (randomized) iterative methods for applications in machine learning and data science. In particular, we will discuss the theoretical basics of stochastic optimization, iterative algorithms for variational inequalities, scalability of algorithms to large datasets, and challenges in distributed optimization, such as decentralized or federated machine learning. We will cover a set of foundational papers and a selection of recent publications.

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.780. Shape and Differential Geometry. 3 Credits.

The purpose of this class is to provide an elementary knowledge of the differential geometry of curves and surfaces, and to place this in relation with the description and characterization of 2D and 3D shapes. Intrinsic local and semi-local descriptors, like the curvature or the second fundamental form will be introduced, with an emphasis on the invariance of these features with respect to rotations, translations, etc. Extension of this point of view to other class of linear transformations will be given, as well as other types of shape descriptors, like moments or medial axes. Recommended Course Background: Calculus III and linear algebra

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.782. Statistical Uncertainty Quantification. 3 Credits.

This course introduces uncertainty quantification (UQ) on mathematical models and data, with emphasis on the use of stochastic processes and probability theory. Topics include computer experiments, designs, conditional probability, Bayesian inference, Gaussian stochastic processes, continuity, reproducing kernel Hilbert space, covariance functions, computer model emulation, parameter estimation, approximation, dynamic linear models, Kalman filter, computation, sensitivity analysis, functional ANOVA, model selection and calibration. Examples of some continuous time processes will be introduced, such as Brownian motion, Brownian bridge, O-U process, with extensions to multi-dimensional input space. Uncertainty analysis of mathematical models will be the focus from both theoretical and computational perspectives. Applications will concentrate on understanding and predicting the behavior of complex systems in science and engineering. Prerequisite EN.553.620 or EN.553.720 Recommended course background: EN.553.630 or EN.553.730.

Prerequisite(s): Students may take EN.550.782 or EN.553.782, but not both.

EN.553.783. Reliability Analysis. 3 Credits.

Reliability is the likelihood that an item will successfully perform to its specified requirements for a stated period of time and understanding its concepts has many applications within various scientific and engineering disciplines. Designed mainly for beginning level graduate students, this course consists of three major components. First, we will revisit some probability principles which will serve as the foundation for this course. Next, we will explore common lifetime models, model selection, and model fitting methods. Finally, we will look at reliability from a systems perspective where the focus will be on system reliability. Students are expected to present their findings on the applications on reliability presented in published works and/or via course projects. Recommended course background: EN.553.620.

EN.553.784. Mathematical Foundations of Computational Anatomy. 3 Credits.

The course will provide fundamental concepts and methods that pertain the analysis of the variation of anatomical shapes extracted from medical images. It will review basic properties of the most important shape representations (landmark, curves, surfaces, images...), describe distances and discrepancy measures that allow for their comparison, and introduce nonlinear optimal control methods that underlie the Large Deformation Diffeomorphic Metric Mapping (LDDMM) family of registration algorithms. The course will then discuss shape averaging methods and template-centered representations for the analysis of shape datasets. Recommended Course Background: Optimization (EN.553.361 or higher) and (AS.110.202 OR AS.110.211 or higher) AND AS.110.302 or higher.

EN.553.785. Asymptotic Analysis. 3 Credits.

Asymptotic analysis is a branch of mathematics that emphasizes finding approximate solutions for either small or large parameters, which have many benefits in various scientific and engineering disciplines. This is because, due to the complexity and mathematical formulation of the problem, analytical solutions are either difficult to obtain or impractical. The goal of this course is to introduce students to some of the most frequently used methods consisting of the following main components. First, an introduction to asymptotic sequences and expansions will be provided as well as some common techniques to obtaining asymptotic expansions on integrals. Next, some common transforms and their inverses will be introduced as well as techniques on finding the asymptotic representation of their inverses. Finally, we will examine some techniques for finding asymptotic representations of solutions resulting from ordinary differential equations. Throughout this course students will also be introduced to some special functions as practical examples to demonstrate how these techniques can be applied to provide robust approximations. Recommended Course Background: Differential Equations and either of the following courses AS.110.405, 110.311, or 110.607.

EN.553.790. Neural Networks and Feedback Control Systems. 2 Credits.

This roundtable course is an introduction to two related areas: neural networks (NNs) and control systems based on the use of feedback. Artificial NNs are effective conceptual and computational vehicles for many important applications; feedback control is relevant to virtually all natural and human-made systems. NNs are applied in areas such as system modeling and control, function approximation, time-series filtering/prediction/smoothing, speech/image/signal processing, and pattern recognition. Topics to be covered for NNs include network architecture, learning algorithms, and applications. Specific NNs discussed include perceptrons, feedforward networks with backpropagation, and recurrent networks. This course also provides an introduction to feedback control systems, including the role of feedback in regulating systems and in achieving stability in systems. We consider stochastic (noise) effects in feedback systems. We also consider the interface of NNs and control by discussing how NNs are used in building modern control systems in problems where standard methods are infeasible. Recommended Course Background: Matrix theory, differential equations, and a graduate course in probability and statistics.

EN.553.791. Internship - Financial Mathematics. 2 Credits.

This course is open only to AMS department master's students.

EN.553.792. Matrix Analysis and Linear Algebra. 4 Credits.

A second course in linear algebra with emphasis on topics useful in analysis, economics, statistics, control theory, and numerical analysis. Review of linear algebra, decomposition and factorization theorems, positive definite matrices, norms and convergence, eigenvalue location theorems, variational methods, positive and nonnegative matrices, generalized inverses. Prerequisite: one semester of real analysis. **Prerequisite(s):** Students may take EN.550.692 or EN.553.792, but not both.

EN.553.793. Turbulence Theory. 3 Credits.

An advanced introduction to turbulence theory for graduate students in the physical sciences, engineering and mathematics. Both intuitive understanding and exact analysis of the fluid equations will be stressed. Previous familiarity with fluid mechanics is not required, although it could be helpful.

EN.553.794. Turbulence Theory II. 3 Credits.

This course will continue the theoretical investigation of fluid turbulence, directly following on from EN.550.693. Topics to be considered are turbulent vortex dynamics, Lagrangian dynamics, and special topics such as wall-bounded turbulence, free shear flows, two-dimensional and quasigeostrophic turbulence, MHD turbulence, etc. Cross-listed with Physics

EN.553.795. Matrix Analysis and Linear Algebra II. 3 Credits.

Additional topics in linear algebra, with emphasis on ideas useful in analysis, economics, statistics, control theory, and numerical analysis, and building on the material of EN.553.792. Singular value inequalities, perturbation of singular subspaces and eigenspaces, field of values, inertia, Kronecker and Hadamard products, matrix equations, matrix functions. Prerequisites: EN.553.792

Prerequisite(s): EN.553.792

Area: Engineering, Quantitative and Mathematical Sciences

EN.553.797. Introduction to Control Theory and Optimal Control. 3 Credits.

A control system is a dynamical system on which one can act through a parameter that can be chosen freely at any point in time. In this class, we will be interested in two main problems. The first one is controllability, which studies conditions for the existence of controls allowing an initial point to be driven to any other point. The second one is optimal control, in which we will study methods to minimize a certain cost over all possible controls, possibly with endpoint constraints. Such problems have many applications in engineering: crossing a river with minimal fuel, planning trajectories of rocket engines etc. Recommended Course Background: Multivariate Calculus, Linear Algebra, Differential Equations. Some familiarity with Optimization is recommended, but not mandatory.

EN.553.799. Topics In Applied Math. 3 Credits.

Machine learning systems have huge capabilities, and they are increasingly being deployed in many real-world applications. Therefore, it is critical to make sure that they are safe and trustworthy. This course focuses on understanding aspects regarding fairness, privacy, explainability, and robustness of machine learning models. The course will cover a list of recent research papers in the field, featuring practical aspects as well as mathematical aspects of these topics. The course not only focuses on the theory of fairness, privacy, explainability, and robustness of machine learning models, but also it aims to develop students' communication skills.

EN.553.800. Dissertation Research. 3 - 20 Credits.**EN.553.801. Department Seminar. 1 Credit.**

A variety of topics discussed by speakers from within and outside the university. Required of all resident department graduate students.

EN.553.802. Graduate Independent Study. 3 Credits.**EN.553.804. Approved External Coursework. 3 - 20 Credits.****EN.553.806. Capstone Experience in Data Science. 3 - 10 Credits.**

Project work for Data Science Master's students. Arranged individually between students and faculty.

Area: Quantitative and Mathematical Sciences

EN.553.809. Master's Research. 3 - 10 Credits.

Reading, research, or project work for Master's level students. Arranged individually between students and faculty.

EN.553.810. Probability & Statistics. 1 - 4 Credits.

Prerequisite(s): EN.553.721

EN.553.847. Financial Mathematics Masters Seminar. 1 Credit.

This course is only open to students enrolled in the MSE in Financial Mathematics program. Advanced topics chosen according to the interests of the instructor and graduate students. The course will focus on recent research articles in the financial mathematics literature.

EN.553.861. Nonsmooth Optimization Seminar. 3 Credits.

Readings and seminar in nonsmooth optimization. Topics may include nonsmooth, nonconvex analysis (generalized gradient and subdifferentials) and nonsmooth, nonconvex optimization methods.